

INFLUENCE OF ANTICLIMBING DEVICE ON THE VARIATION OF LOADS ON WHEELS IN DIESEL ELECTRIC 4000 HP

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Dispozitivul anticabraj introduce sarcini suplimentare pe roțile osiilor locomotivelor. În lucrare se prezintă variația acestor sarcini, funcție de datele constructive ale locomotivei Diesel electrice de 4000 CP.

The anticlimbing device inserts additional tasks over axles' wheels of locomotives. In this study, the variation of these tasks depending on the construction data of Diesel-electric locomotive of 4000 HP is presented.

Keywords : the anticlimbing device

1. Introduction

Axles' individual action system introduces in mounted axle – suspense - bogie frame ensemble, forces and moments that determine a redistribution of tasks between the axles of the bogie.

2. Forces introduced by the anticlimbing device

At the box the reactions from the anticlimbing device act (fig. 1.a). From the equations of equilibrium of the box one can calculate the reactions ΔC_1 and ΔC_2 from vertical fulcrum points of the drop box on bogies:

$$\Delta C_1 = N_1 * \frac{a_1 + a_L}{a_L} + N_2 * \frac{a_2}{a_L} \quad (1)$$

$$\Delta C_2 = N_2 * \frac{a_L - a_2}{a_L} - N_1 * \frac{a_1}{a_L} \quad (2)$$

where : N_1 – force on the first bogie to pivot distance p_1 ; N_2 - force on the second bogie to pivot distance p_2

The forces ΔC_1 and ΔC_2 load bogies through their components $\frac{\Delta C_1}{2}$ and

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$\frac{\Delta C_2}{2}$ from points 7, 8 and 10, 11 of vertical fulcrum of the box on bogies.

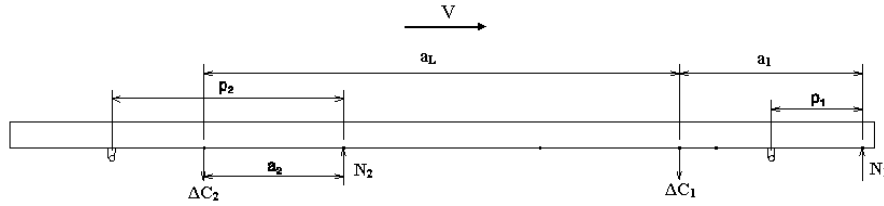
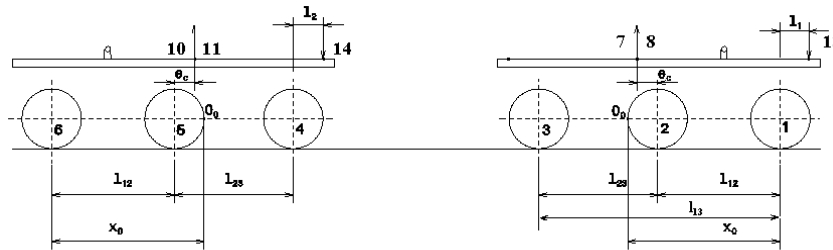


Fig. 1.a



11	$-(x_0 - l_{12} - e_c)$	$-b_0$	h_{11}	0	$\frac{\Delta C_2}{2}$	0
13	$x_0 + l_1$	0	h_{13}	0	$-N_1$	0
14	$-(x_0 - l_{13} - l_2)$	0	h_{14}	0	$-N_2$	0

$$\begin{aligned}
 [r_0]_7 &= \begin{bmatrix} 0 & 1 & 0 \\ 0 & b_0 & 0 \\ h_7 & -(x_0 - l_{12} - e_c) & 1 \end{bmatrix} & [r_0]_8 &= \begin{bmatrix} 0 & 1 & 0 \\ 0 & -b_0 & 0 \\ h_8 & -(x_0 - l_{12} - e_c) & 1 \end{bmatrix} \\
 [r_0]_{10} &= \begin{bmatrix} 0 & 1 & 0 \\ 0 & b_0 & 0 \\ h_{10} & -(x_0 - l_{12} - e_c) & 1 \end{bmatrix} & [r_0]_{11} &= \begin{bmatrix} 0 & 1 & 0 \\ 0 & b_0 & 0 \\ h_{11} & (x_0 - l_{12} - e_c) & 1 \end{bmatrix} \\
 [r_0]_{13} &= \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0 \\ h_{13} & -(x_0 - l_1) & 1 \end{bmatrix} & [r_0]_{14} &= \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0 \\ h_{14} & (x_0 - l_{13} - l_2) & 1 \end{bmatrix}
 \end{aligned}$$

The values of loads introduced on the bogies by the anticlimbing device are composed of:

$$\begin{aligned}
 \{P_7\}_N &= \begin{bmatrix} 0 \\ \frac{\Delta C_1}{2} \\ 0 \end{bmatrix} ; & \{P_8\}_N &= \begin{bmatrix} 0 \\ \frac{\Delta C_1}{2} \\ 0 \end{bmatrix} ; & \{P_{10}\}_N &= \begin{bmatrix} 0 \\ \frac{\Delta C_2}{2} \\ 0 \end{bmatrix} \\
 \{P_{11}\}_N &= \begin{bmatrix} 0 \\ \frac{\Delta C_2}{2} \\ 0 \end{bmatrix} ; & \{P_{13}\}_N &= \begin{bmatrix} 0 \\ -N_1 \\ 0 \end{bmatrix} ; & \{P_{14}\}_N &= \begin{bmatrix} 0 \\ -N_2 \\ 0 \end{bmatrix}
 \end{aligned}$$

Bringing back torsion in O_0 of these loads are:

For bogie I

$$\{T_{0I}\}_N = [r_0]_7 * \{P_7\}_N + [r_0]_8 * \{P_8\}_N + [r_0]_{13} * \{P_{13}\}_N$$

$$\begin{aligned}
 \{T_{0I}\}_N &= \begin{bmatrix} 0 & 1 & 0 \\ 0 & b_0 & 0 \\ h_7 & -(x_0 - l_{12} - e_c) & 1 \end{bmatrix} \begin{bmatrix} 0 \\ \frac{\Delta C_1}{2} \\ 0 \end{bmatrix} + \begin{bmatrix} 0 & 1 & 0 \\ 0 & -b_0 & 0 \\ h_8 & -(x_0 - l_{12} - e_c) & 1 \end{bmatrix} \begin{bmatrix} 0 \\ \frac{\Delta C_1}{2} \\ 0 \end{bmatrix} + \\
 &+ \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0 \\ h_{13} & -(x_0 + l_1) & 1 \end{bmatrix} \begin{bmatrix} 0 \\ -N_1 \\ 0 \end{bmatrix}
 \end{aligned}$$

$$\{T_{0I}\}_N = \begin{bmatrix} -N_1 + \Delta C_1 \\ 0 \\ (x_0 + l_1)N_1 - (x_0 - l_{12} - e_c)\Delta C_1 \end{bmatrix} \quad (3)$$

For bogie II

$$\begin{aligned} \{T_{0II}\}_N &= [r_0]_{10} * \{P_{10}\}_N + [r_0]_{11} * \{P_{11}\}_N + [r_0]_{14} * \{P_{14}\}_N \\ \{T_{0II}\}_N &= \begin{bmatrix} 0 & 1 & 0 \\ 0 & b_0 & 0 \\ h_{10} & (x_0 - l_{12} - e_c) & 1 \end{bmatrix} \begin{bmatrix} 0 \\ \frac{\Delta C_2}{2} \\ 0 \end{bmatrix} + \begin{bmatrix} 0 & 1 & 0 \\ 0 & -b_0 & 0 \\ h_{11} & (x_0 - l_{12} - e_c) & 1 \end{bmatrix} \begin{bmatrix} 0 \\ \frac{\Delta C_2}{2} \\ 0 \end{bmatrix} \\ &+ \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0 \\ h_{14} & (x_0 - l_{13} - l_2) & 1 \end{bmatrix} \begin{bmatrix} 0 \\ -N_2 \\ 0 \end{bmatrix} \\ \{T_{0II}\}_N &= \begin{bmatrix} -N_2 + \Delta C_2 \\ 0 \\ -(x_0 + l_{13} - l_2)N_2 + (x_0 - l_{12} - e_c)\Delta C_2 \end{bmatrix} \end{aligned} \quad (4)$$

Considering expression of x_0 given by relation (5).

$$x_o = \frac{l_{12} + l_{13}}{3} \quad (5)$$

$$x_o = \frac{1950 + 4100}{3} = 2016,66mm$$

also by relations (1) and (2), result: for bogie I:

$$\{T_{0I}\}_N = \begin{bmatrix} \frac{a_1}{a_L} N_1 + \frac{a_2}{a_L} N_2 \\ 0 \\ N_1(l_{12} + l_1 + e_c) - \left(\frac{l_{23} - l_{12}}{3} - e_c\right) \left(\frac{a_1}{a_L} * N_1 + \frac{a_2}{a_L} * N_2\right) \end{bmatrix} \quad (6)$$

for bogie II:

$$\{T_{0II}\}_N = \begin{bmatrix} -\left(\frac{a_1}{a_L} * N_1 + \frac{a_2}{a_L} * N_2\right) \\ 0 \\ N_2(l_{23} + l_2 - e_c) - \left(\frac{l_{23} - l_{12}}{3} - e_c\right) \left(\frac{a_1}{a_L} * N_1 + \frac{a_2}{a_L} * N_2\right) \end{bmatrix} \quad (7)$$

3.-Variation of loads on wheels determined by anticlimbing device

Loads introduced in ellipses by anticlimbing device are:

For bogie I:

$$\{P'_s\}_I = [A]_I * \{T_{0I}\}_N = \begin{bmatrix} \frac{1}{3} & -\frac{1}{3b_0} & -\frac{1}{l_{13}+l_{23}} \\ \frac{1}{3} & \frac{1}{3b_0} & -\frac{1}{l_{13}+l_{23}} \\ \frac{1}{6} & -\frac{1}{6b_0} & +\frac{1}{l_{13}+l_{23}} \\ \frac{1}{6} & \frac{1}{6b_0} & +\frac{1}{l_{13}+l_{23}} \end{bmatrix} \begin{bmatrix} P_{zol} \\ M_{xol} \\ M_{yol} \end{bmatrix}_N = \begin{bmatrix} P'_{a1} \\ P'_{a2} \\ P'_{31s} \\ P'_{32s} \end{bmatrix}_N \quad (8)$$

Performing calculations and taking into account the relation (6) results:

$$P'_{a1} = \frac{l_{23} - e_c}{l_{13} + l_{23}} \left(\frac{a_1}{a_L} * N_1 + \frac{a_2}{a_L} * N_2 \right) - \frac{l_{12} + l_1 + e_c}{l_{13} + l_{23}} * N_1$$

$$P'_{a2} = P'_{a1}$$

$$P'_{31s} = \frac{1}{2} * \frac{l_{12} + 2e_c}{l_{13} + l_{23}} \left(\frac{a_1}{a_L} * N_1 + \frac{a_2}{a_L} * N_2 \right) + \frac{l_{12} + l_1 + e_c}{l_{13} + l_{23}} * N_1$$

$$P'_{32s} = P'_{31s}$$

For bogie II:

$$\{P'_s\}_{II} = [A]_{II} * \{T_{0II}\}_N = \begin{bmatrix} \frac{1}{6} & -\frac{1}{6b_0} & -\frac{1}{l_{13}+l_{23}} \\ \frac{1}{6} & \frac{1}{6b_0} & -\frac{1}{l_{13}+l_{23}} \\ \frac{1}{3} & -\frac{1}{3b_0} & +\frac{1}{l_{13}+l_{23}} \\ \frac{1}{3} & \frac{1}{3b_0} & +\frac{1}{l_{13}+l_{23}} \end{bmatrix} \begin{bmatrix} P_{zol} \\ M_{xol} \\ M_{yol} \end{bmatrix}_N = \begin{bmatrix} P'_{41s} \\ P'_{42s} \\ P'_{f1} \\ P'_{f2} \end{bmatrix}_N \quad (9)$$

$$P'_{41s} = -\frac{1}{2} * \frac{l_{12} + 2e_c}{l_{13} + l_{23}} \left(\frac{a_1}{a_L} * N_1 + \frac{a_2}{a_L} * N_2 \right) - \frac{l_{12} + l_2 - e_c}{l_{13} + l_{23}} * N_2$$

$$P'_{42s} = P'_{41s}$$

$$P'_{f1} = \frac{l_{23} - e_c}{l_{13} + l_{23}} \left(\frac{a_1}{a_L} * N_1 + \frac{a_2}{a_L} * N_2 \right) + \frac{l_{23} + l_2 - e_c}{l_{13} + l_{23}} * N_2$$

From the distribution of these forces on the axles' spindles results additional loads on axles' wheels given by anticlimbing device:

For bogie I:

$$\{P'_{ij}\}_I = \begin{bmatrix} P'_{11} \\ P'_{12} \\ P'_{21} \\ P'_{22} \\ P'_{31} \\ P'_{32} \end{bmatrix} = \begin{bmatrix} \frac{P'_{a1}}{2} \\ \frac{P'_{a2}}{2} \\ \frac{P'_{a1}}{2} \\ \frac{P'_{a2}}{2} \\ \frac{P'_{a2}}{2} \\ P'_{31s} \\ P'_{32s} \end{bmatrix} \quad (10)$$

For bogie II:

$$\{P'_{ij}\}_{II} = \begin{bmatrix} P'_{41} \\ P'_{42} \\ P'_{51} \\ P'_{52} \\ P'_{61} \\ P'_{62} \end{bmatrix} = \begin{bmatrix} P'_{41s} \\ P'_{42s} \\ \frac{P'_{f1}}{2} \\ \frac{P'_{f2}}{2} \\ \frac{P'_{f1}}{2} \\ \frac{P'_{f2}}{2} \end{bmatrix} \quad (11)$$

The constructive data of the analyzed locomotive are presented below:

$$a_1 = 2725 \text{ mm} ; a_2 = 2915 \text{ mm} ; l_1 = 720 \text{ mm}$$

$$l_2 = 820 \text{ mm} ; N_1 = 5740 \text{ daN} ; N_2 = 5410 \text{ daN}$$

The vector of additional loads which are introduced on the wheels by the anticlimbing device is :

For bogie I:

$$\{P'_{ij}\}_I = \begin{bmatrix} -785 \text{ daN} \\ -785 \text{ daN} \\ -785 \text{ daN} \\ -785 \text{ daN} \\ 2961 \text{ daN} \\ 2961 \text{ daN} \end{bmatrix} \quad (12)$$

For bogie II:

$$\{P'_{ij}\}_{II} = \begin{bmatrix} -2981,7 & daN \\ -2981,7 & daN \\ +795,3 & daN \\ +795,3 & daN \\ +795,3 & daN \\ +795,3 & daN \end{bmatrix} \quad (13)$$

4. Variation of loads on wheels at anticlimbing device locomotive

Variation of loads on wheels at anticlimbing device locomotive results from the relations:

$$\{P_{ij}\}_I = \begin{bmatrix} P_{11} \\ P_{12} \\ P_{21} \\ P_{22} \\ P_{31} \\ P_{32} \end{bmatrix} = \begin{bmatrix} \frac{P_{a1} + P_0}{2} \\ \frac{P_{a2} + P_0}{2} \\ \frac{P_{a1} + P_0}{2} \\ \frac{P_{a2} + P_0}{2} \\ \frac{P_{31s} - \frac{P_v}{2}}{2} \\ \frac{P_{32s} - \frac{P_v}{2}}{2} \end{bmatrix} = \begin{bmatrix} c_{11} * F_0 \\ c_{12} * F_0 \\ c_{21} * F_0 \\ c_{22} * F_0 \\ c_{31} * F_0 \\ c_{32} * F_0 \end{bmatrix} \quad \text{and} \quad \{P'_{ij}\}_I = \begin{bmatrix} P'_{11} \\ P'_{12} \\ P'_{21} \\ P'_{22} \\ P'_{31} \\ P'_{32} \end{bmatrix} = \begin{bmatrix} \frac{P'_{a1}}{2} \\ \frac{P'_{a2}}{2} \\ \frac{P'_{a1}}{2} \\ \frac{P'_{a2}}{2} \\ \frac{P'_{31s}}{2} \\ \frac{P'_{32s}}{2} \end{bmatrix} \quad \text{and}$$

respectively

$$\{P_{ij}\}_{II} = \begin{bmatrix} P_{41} \\ P_{42} \\ P_{51} \\ P_{52} \\ P_{61} \\ P_{62} \end{bmatrix} = \begin{bmatrix} \frac{P_{41s} + \frac{P_v}{2}}{2} \\ \frac{P_{42s} + \frac{P_v}{2}}{2} \\ \frac{P_{f1}}{2} - \frac{P_v}{2} \\ \frac{P_{f2}}{2} - \frac{P_v}{2} \\ \frac{P_{f1}}{2} - \frac{P_v}{2} \\ \frac{P_{f2}}{2} - \frac{P_v}{2} \end{bmatrix} = \begin{bmatrix} c_{41} * F_0 \\ c_{42} * F_0 \\ c_{51} * F_0 \\ c_{52} * F_0 \\ c_{61} * F_0 \\ c_{62} * F_0 \end{bmatrix} \quad \text{and} \quad \{P'_{ij}\}_{II} = \begin{bmatrix} P'_{41} \\ P'_{42} \\ P'_{51} \\ P'_{52} \\ P'_{61} \\ P'_{62} \end{bmatrix} = \begin{bmatrix} \frac{P'_{41s}}{2} \\ \frac{P'_{42s}}{2} \\ \frac{P'_{f1}}{2} \\ \frac{P'_{f2}}{2} \\ \frac{P'_{f1}}{2} \\ \frac{P'_{f2}}{2} \end{bmatrix}$$

In this way:

For bogie I:

$$\{\Delta Q_{ij}\}_I = \{P_{ij}\}_I + \{P'_{ij}\}_I$$

$$\{\Delta Q_{ii}\}_I = \begin{bmatrix} \Delta Q_{11} \\ \Delta Q_{12} \\ \Delta Q_{21} \\ \Delta Q_{22} \\ \Delta Q_{31} \\ \Delta Q_{32} \end{bmatrix} = \begin{bmatrix} P_{11} + P'_{11} \\ P_{12} + P'_{12} \\ P_{21} + P'_{21} \\ P_{22} + P'_{22} \\ P_{31} + P'_{31} \\ P_{32} + P'_{32} \end{bmatrix} = \begin{bmatrix} c_{11} * F_0 + \frac{P'_{a1}}{2} \\ c_{12} * F_0 + \frac{P'_{a2}}{2} \\ c_{21} * F_0 + \frac{P'_{a1}}{2} \\ c_{22} * F_0 + \frac{P'_{a2}}{2} \\ c_{31} * F_0 + \frac{P'_{31s}}{2} \\ c_{32} * F_0 + \frac{P'_{32s}}{2} \end{bmatrix}$$

Replacing the constructive data of the locomotive, it results:

$$\{\Delta Q_{ii}\}_I = \begin{bmatrix} +0,235398 * F_0 & -785 & daN \\ +0,235398 * F_0 & -785 & daN \\ +0,235398 * F_0 & -785 & daN \\ +0,235398 * F_0 & -785 & daN \\ -0,441567 * F_0 & +2961 & daN \\ -0,441567 * F_0 & +2961 & daN \end{bmatrix} \quad (14)$$

For bogie II:

$$\{\Delta Q_{ii}\}_{II} = \begin{bmatrix} \Delta Q_{41} \\ \Delta Q_{42} \\ \Delta Q_{51} \\ \Delta Q_{52} \\ \Delta Q_{61} \\ \Delta Q_{62} \end{bmatrix} = \begin{bmatrix} P_{41} + P'_{41} \\ P_{42} + P'_{42} \\ P_{51} + P'_{51} \\ P_{52} + P'_{52} \\ P_{61} + P'_{61} \\ P_{62} + P'_{62} \end{bmatrix} = \begin{bmatrix} c_{41} * F_0 + \frac{P'_{41}}{2} \\ c_{42} * F_0 + \frac{P'_{42}}{2} \\ c_{51} * F_0 + \frac{P'_{f1}}{2} \\ c_{52} * F_0 + \frac{P'_{f2}}{2} \\ c_{61} * F_0 + \frac{P'_{f1}}{2} \\ c_{62} * F_0 + \frac{P'_{f2}}{2} \end{bmatrix}$$

$$\{\Delta Q_{ii}\}_{II} = \begin{bmatrix} +0,441567 * F_0 & -2981,7 & daN \\ +0,441567 * F_0 & -2981,7 & daN \\ -0,235398 * F_0 & +795,3 & daN \\ -0,235398 * F_0 & +795,3 & daN \\ -0,235398 * F_0 & +795,3 & daN \\ -0,235398 * F_0 & +795,3 & daN \end{bmatrix} \quad (15)$$

Variation of loads on wheels is given in the diagram from Fig. 2.

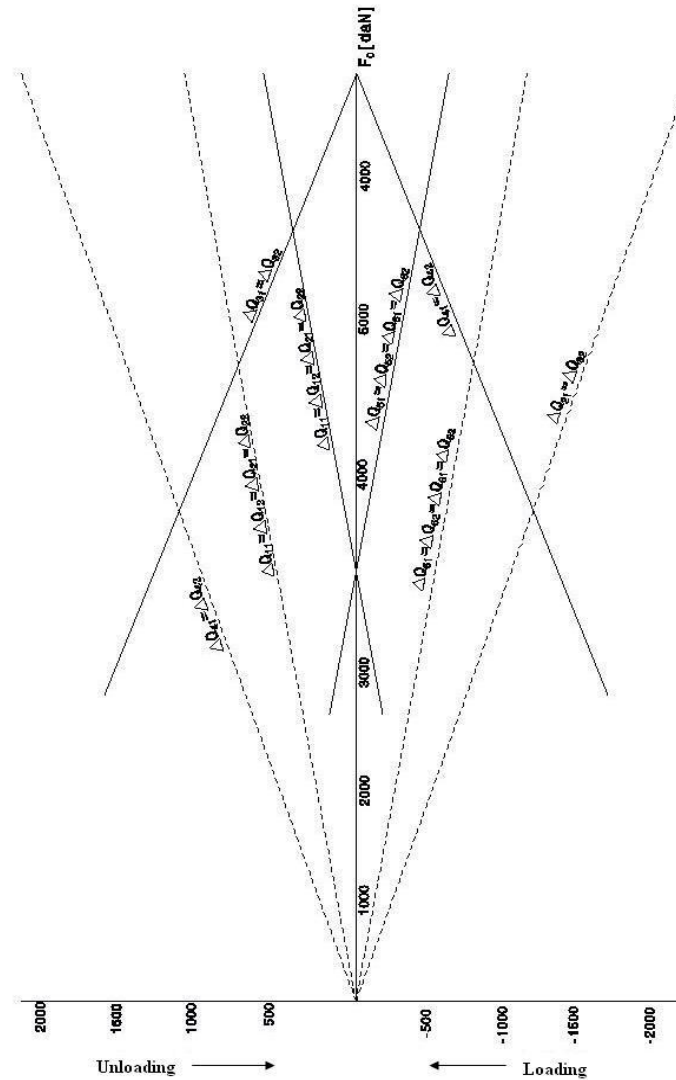


Fig. 2 Variation of loads on wheels

Variation of loads on wheels at anticlimbing device locomotive is represented with continous line and variation of loads on wheels at locomotive without anticlimbing device is represented with dashed line.

5. Conclusions

The anticlimbing device loads bogies in order to produce a decrease of discharge axles 1 and 2 of first bogie, so that the first bogie's II axle (axle number 4 of locomotive).

Consequently, towards the direction of movement in Fig. 1.a, the anticlimbing device introduces a force N_1 on the first bogie at distance p_1 towards the pivotal, distance l_1 towards the first axle and N_2 on II bogie at distance p_2 towards the pivotal, distance l_2 towards axle number 4.

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